

Game Theory and the Economic Way of Thinking

- Game theory is formal economic reasoning applied to situations in which decisions are **interdependent**
- Game theory is a very flexible tool that allows us to develop more precise models of situations that involve **strategic interactions**

Game Theory and the Economic Way of Thinking

- **Formal game theory assumptions:**
 - Players are fully forward looking
 - Players always behave in a manner that gives them the highest payoff
 - Players expect all other players to behave in the same manner

Game Theory and Oligopolies

- Game theory is most commonly applied to oligopolies
- Oligopolies can produce similar **or** differentiated goods (cars, steel, etc)
- Oligopolies are **interdependent** since they compete with only a few other firms

Game Theory and Oligopolies

- Their pricing and output decisions must be strategic to avoid economic losses—their decisions are **mutually interdependent**
- **Game theory helps us analyze their strategies**

Payoff Matrix

- **Payoff matrix:** a table that shows the outcome of every choice by every player, given the possible choices of all other players
 - The payoff matrix has three elements:
 1. Players
 2. Strategies
 3. Payoffs

Payoff Matrix

This is a payoff matrix for Firm A and Firm B and their profits. The first entry in each cell column represents Firm A's profits and the second entry in each cell represents Firm B's profits.

		Firm B	
		Raise Price	Lower Price
Firm A	Raise Price	\$100, \$80	\$80, \$90
	Lower Price	\$90, \$75	\$70, \$80

Payoff Matrix

The easiest way to analyze which strategy is best is to start with one player at a time. We will “box” Firm A’s strategies and analyze them first.

		Firm B	
		Raise Price	Lower Price
Firm A	Raise Price	\$100, \$80	\$80, \$90
	Lower Price	\$90, \$75	\$70, \$80

Payoff Matrix

Step 1: We will use an **X** to identify which strategy is best for **Firm A**.

- If Firm B raises its price, Firm A can raise its price for \$100 in profit, or lower its price for \$90 in profit.
- If Firm B lowers its price, Firm A can raise its price for \$80 in profit, or lower its price for \$70 in profit.

		Firm B	
		Raise Price	Lower Price
Firm A	Raise Price	X \$100, \$80	X \$80, \$90
	Lower Price	\$90, \$75	\$70, \$80

Payoff Matrix

Step 2: We will use a ✓ to identify which strategy is best for **Firm B**.

- If Firm A raises its price, Firm B can raise its price for \$80 in profit, or lower its price for \$90 in profit.
- If Firm A lowers its price, Firm B can raise its price for \$75 in profit, or lower its price for \$80 in profit.

		Firm B	
		Raise Price	Lower Price
Firm A	Raise Price	X \$100, \$80	X ✓ \$80, \$90
	Lower Price	\$90, \$75	\$70, \$80 ✓

Payoff Matrix

What is the best strategy for each Firm given the other player's choice?

- Firm A's best strategy is to **raise price**.
- Firm B's best strategy is to **lower price**.

		Firm B	
		Raise Price	Lower Price
Firm A	Raise Price	X \$100, \$80	X ✓ \$80, \$90
	Lower Price	\$90, \$75	\$70, \$80 ✓

Payoff Matrix

Firm B

Firm A

		Raise Price	Lower Price
Raise Price	<p>X</p> <p>\$100, \$80</p>	<p>X ✓</p> <p>\$80, \$90</p>	
Lower Price	<p>\$90, \$75</p>	<p>✓</p> <p>\$70, \$80</p>	
	<p>X</p> <p>Raise, Raise</p>	<p>X ✓</p> <p>Raise, Lower</p>	
	<p>Lower, Raise</p>	<p>✓</p> <p>Lower, Lower</p>	

Dominant Strategy

- In the previous example, both Firm A and B have a **dominant strategy**: the decision (strategy) you will make regardless of what your opponent does
- When looking at two firms, they **may or may not** have a dominant strategy
- If there is not a dominant strategy, the firm is **dependent** on what the other firm does

Dominant Strategy

- We look at the rows and columns to determine a dominant strategy.
- Since Firm A will raise its price no matter what Firm B does, its dominant strategy is to raise its price. Since Firm B will lower its price no matter what Firm A does, its dominant strategy is to lower its price.

	Firm B	
Firm A	X Raise, Raise	X ✓ Raise, Lower
	Lower, Raise	Lower, Lower ✓

Nash Equilibrium

- A **Nash equilibrium** means no player can improve his or her payoff by changing his/her strategy on their own
 - A Nash equilibrium **doesn't** have to be the solution that is jointly best for all players
 - This appears when there is an “x” and a “✓” in one of the boxes of the matrix—this would be the decision each player/firm makes

Nash Equilibrium

- Below, there is a Nash equilibrium:

		Firm B	
		Raise Price	Lower Price
Firm A	Raise Price	X \$100, \$80	X ✓ \$80, \$90
	Lower Price	\$90, \$75	\$70, \$80 ✓

The Prisoner's Dilemma

- The **prisoner's dilemma** is a 2 person **non-cooperative** game that demonstrates the difficulty of cooperative behavior

The Prisoner's Dilemma: Example

- “If **both you and the other prisoner confess**, instead of being sentenced to the **maximum 10 years** in prison, the two of you will each serve only **5 years** in jail. Further, if **you confess and the other prisoner does not confess**, in exchange for your serving as a witness for the prosecution, we will drop the charges for the lesser felony, and **you will be set free**. If, however, **you don't confess and the other suspect does**, you will be sentenced to the **maximum 10 years in prison**. If neither confesses, both will be charged with the lesser felony and serve 6 months.”

Application: The Prisoner's Dilemma

This is a payoff matrix for Prisoner A and B. The first entry in each cell column represents Prisoner A's options and the second entry in each cell represents Prisoner B's options.

		B	
		CONFESS	DON'T CONFESS
A	CONFESS	5 years for A, 5 years for B	A goes free, 10 years for B
	DON'T CONFESS	10 years for A, B goes free	6 months for A, 6 months for B

Application: The Prisoner's Dilemma

The easiest way to analyze is to start with one player at a time. We will “box” Prisoner A’s strategies and analyze them first.

		B	
		CONFESS	DON'T CONFESS
A	CONFESS	5 years for A, 5 years for B	A goes free, 10 years for B
	DON'T CONFESS	10 years for A, B goes free	6 months for A, 6 months for B

Application: The Prisoner's Dilemma

Step 1: We will use an **X** to identify which strategy is best for Prisoner A.

- If Prisoner B confesses, Prisoner A can confess for 5 years or not confess for 10 years.

- If Prisoner B does not confess, Prisoner A can confess and go free or don't confess for 6 months.

		B	
		CONFESS	DON'T CONFESS
A	CONFESS	<p style="text-align: center;">X</p> <p>5 years for A, 5 years for B ✓</p>	<p style="text-align: center;">X</p> <p>A goes free, 10 years for B</p>
	DON'T CONFESS	<p>10 years for A, B goes free ✓</p>	<p>6 months for A, 6 months for B</p>

Application: The Prisoner's Dilemma

Step 2: We will use a ✓ to identify which strategy is best for Prisoner B.

- If Prisoner A confesses, Prisoner B can confess for 5 years or not confess for 10 years.

- If Prisoner A does not confess, Prisoner B can confess and go free or don't confess for 6 months.

		B	
		CONFESS	DON'T CONFESS
A	CONFESS	<p style="text-align: center;">X</p> <p>5 years for A, 5 years for B ✓</p>	<p style="text-align: center;">X</p> <p>A goes free, 10 years for B</p>
	DON'T CONFESS	<p>10 years for A, B goes free ✓</p>	<p>6 months for A, 6 months for B</p>

Application: The Prisoner's Dilemma

- What is the best strategy for each Prisoner given the other Prisoner's choice? What is the outcome?
- Here, 5 years for Prisoner A and 5 years for Prisoner B is the best outcome.

		B	
		CONFESS	DON'T CONFESS
A	CONFESS	X 5 years for A, 5 years for B ✓	X A goes free, 10 years for B
	DON'T CONFESS	10 years for A, B goes free ✓	6 months for A, 6 months for B

Application: The Prisoner's Dilemma

- **Why???**
 - Although **not confessing** is the best outcome for prisoner A and B, they cannot count on each other not to confess
 - As a result, the best combined outcome for them would be for each to confess and serve 5 years

Example: The Game Theory Framework

- **Four “A” students partied the night before an exam and slept through the exam**
- **They tell the professor that the reason they missed the exam was that they were all in a car that had a flat tire**
- **The professor lets them make up the exam**

Example: The Game Theory Framework

- The exam had two questions: an essay relating to the course material and a screening question... which tire was flat?
 - This is a **screening question**: its purpose is to reveal strategic information about the person who answers

An Overview of Game Theory as a Tool in Studying Strategic Interaction

- A **non-cooperative game** is a game in which each player is out for him- or herself and agreements are either not possible or not enforceable
- **Cooperative games** are games in which players can form coalitions and the coalition can enforce its will on its members

An Overview of Game Theory as a Tool in Studying Strategic Interaction

- **Sequential games** are games where players make decisions one after another
 - **Example:** Chess
- **Simultaneous move games** are games where players make their decisions at the same time as other players (for example, the prisoner's dilemma)

Strategies of Players

- **Backward induction:** you begin with a desired outcome and then determine the decisions that could have led you to that outcome

Strategies of Players

- A **dominant strategy** is a strategy that is preferred by a player regardless of the opponent's move
 - Ex: Prisoner's dilemma
- A **mixed strategy** is a strategy of choosing randomly among moves
 - Ex: Rock, paper, scissors

Informal Game Theory and Modern Behavioral Economics

- Informal game theory is often called **behavioral game theory** because it relies on empirical observation, not deductive logic alone, to determine the likely choices of individuals
 - So...it provides a framework for approaching questions

Behavioral Economics and Game Theory

- **Behavioral economists use experiments and have people play the formal games to explore the validity of the assumptions in formal game theory and how they might be revised**

Loss Aversion, Incorrect Inference, and Framing Effects

- **Framing effects** are the tendency of people to base their choices on how the choice is presented
 - **An early-bird special is a better advertisement than a surcharge for peak-time meals**
 - **Would you choose option A of saving 200 of 600 lives, or option B that will end lives of 400 of 600?**

Chapter Summary

- **Game theory is a flexible approach that is useful when decisions are interdependent**
- **In the prisoner's dilemma game both players have a dominant strategy that leads to a jointly undesirable outcome**
- **A payoff matrix provides a summary of each player's strategies and how the outcomes of their choices depend on the actions of the other players**
- **A Nash equilibrium is an equilibrium of a game that results from a non-cooperative game when each player plays his or her best strategy**

Chapter Summary

- **A dominant strategy is preferred regardless of one's opponent's move. A mixed strategy is choosing randomly**
- **Behavioral economics examines deviations between formal game theoretical predictions and actual outcomes of games**
- **Loss aversion and framing effects are examples of findings in behavioral economics that challenge the traditional model's predictions**
- **The traditional model remains relevant because it only takes a few people to realize that money has been left on the table for the results of the standard model to hold**